## Exercise 8 - Machine Learning II - 2016

Please send your submissions (runnable code, plots and written answers) via email to weis@ccc.cs.unifrankfurt.de until Tuesday June 14th 2016. One submission per student. Prepare to present your solutions in the exercise session. Students that are not able to explain their solutions may not be given credit on their submissions.

## 1 Neural Networks implementation (5 Points)

In this exercise you will implement and train a small Neural Network with backpropagation. Consider the following data:

| Input |  |  | Output |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 0 |
| 1 | 1 | 1 | 1 |
| 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 |

The goal is to predict the output, given the three inputs, using the following network architecture:


Lets use the following definitions and variables in this exercise:

| Variable | Definition |
| :---: | :--- |
| X | Input dataset matrix (each row is a training example) |
| y | Output dataset matrix (each row is a traning example) |
| 10 | First layer of the net (specified by input data) |
| l | Second layer of the net (usually called hidden, here:output) |
| w 0 | Weights of the first layer, connection first to second layer |
| $*$ | Elementwise multiplication |
| - | Elementwise subtraction |
| x.dot(y) | Dot product |
| As you already know, you need to implement the following steps: |  |

1. Implement a function that returns the logistic (hint: $\frac{1}{1+e^{-x}}$ ) as nonlinearity, as well as it's derivative given $\mathrm{x}(\operatorname{hint}: \operatorname{logistic}(x) *(1-\operatorname{logistic}(x)))$
2. Represent input and output dataset as numpy arrays
3. Initialize the weights randomly as numpy array (use np.random.seed(1) beforehand to get a deterministic random sequence for comparison reasons)
4. In a loop (1000 times):

- Populate the first layer with the training data (all at once, full batch)
- Compute the forward-pass (prediction) (hint: logistic(np.dot()))
- Compute the error w.r.t. the given outputs
- Perform the weight-update (hint: multiply error with derivative of predicted values)
- Visualize the current error (np.sum(np.abs(error)))


## 2 Neural Networks - Questions (5 Points)

- Why do we pass the output of $l 0 * w 0$ through the nonlinearity?
- What is the meaning of weighting the error with the derivative of the output prediction (what happens for small/large errors)?
- How could you automatically stop the training process without specifying a constant number of iterations?
- As you noticed, the first variable is directly correlated with the output, we have a linear mapping of input to output. How can the network structure be changed to handle nonlinear problems?
- What are the differences of Stochastic Gradient Descent to the method used in our example?

